

Unit 5 – Analysis of Paired Data

1. Scatter diagram : x = horizontal scale , y = vertical scale

2. Calculate the Linear Correlation Coefficient

ρ = population linear correlation coefficient

r = sample linear correlation coefficient (r estimates ρ)

$$r = \frac{n\sum(xy) - (\sum x)(\sum y)}{\sqrt{n(\sum x^2) - (\sum x)^2} \sqrt{n(\sum y^2) - (\sum y)^2}} \quad (\text{round off to 3 decimal places})$$

Test r for statistical significance

Method 1 : Hypothesis test

- Write the claim about ρ .
 - $\rho \neq 0$: “a correlation exists” (default claim)
 - $\rho = 0$: “no correlation exists”
 - $\rho > 0$: “a positive correlation exists”
 - $\rho < 0$: “a negative correlation exists”

2. Write the opposite of the claim.

3. Identify H_0 and H_1 . (H_0 MUST CONTAIN EQUALITY)

4. Choose α and identify the test type. (look at H_1)

5. Find t_{crit} using Table A-3 Row = d.o.f. = $n - 2$ (bivariate)
Column = α and test type

6. Calculate $t_{test} = \frac{r}{\sqrt{\frac{1-r^2}{n-2}}}$

7. Draw the bell curve to compare t_{test} and t_{crit} .

8. Reject H_0 if t_{test} falls in the critical region.

9. Write the conclusion.

Method 2 : Use Table A-6 on Page 780

1. Calculate r

2. On Table A-6 look at the row for n

3. If $r >$ critical value, the results are statistically significant.

3. If r is significant, find the regression equation (Line of Best Fit) :

for a population : $y = \beta_1 x + \beta_0$

for a sample : $\hat{y} = b_1 x + b_0$

x = independent variable

y = dependent variable

$$b_1 = \text{slope of the line (estimates } \beta_1) = \frac{n(\sum xy) - (\sum x)(\sum y)}{n(\sum x^2) - (\sum x)^2}$$

$$b_0 = y \text{ intercept (estimates } \beta_0) = \frac{(\sum y)(\sum x^2) - (\sum x)(\sum xy)}{n(\sum x^2) - (\sum x)^2}$$

round off b_1 and b_0 to 3 significant digits

4. Choose 2 different values for x between the minimum and maximum x values in your data.

5. Calculate \hat{y} for the 2 values of x chosen using the regression equation.

Result : Two new ordered pairs $(x_1, \hat{y}_1), (x_2, \hat{y}_2)$

6. Plot the 2 new ordered pairs on the scatter diagram and draw a line running through them.
(this plots the regression line against the data)

